

We want to make a GeoGebra worksheet to explore the solution to

$$\frac{dy}{dt} = ky \left(1 - \frac{y}{L}\right)$$

where $y(t)$ is the population as a function of time t , k is the coefficient of growth, and L is the **carrying capacity**.

Theorem: The solution to the differential equation is

$$y(t) = \frac{L}{1 + be^{-kt}}$$

where b is some constant of integration.

1. Make 3 sliders: L , b , and k with the **Slider Tool** (2nd from right). You can edit these later by selecting “Object Properties” either in the graph view or the Algebra view.
 - (a) Name: “ L ”, Min:1, Max: 50, Increment: 1
 - (b) Name: “ b ”, Min:0, Max: 40, Increment: 0.5
 - (c) Name: “ k ”, Min:0, Max: 0.2, Increment: 0.01
2. In the “Input” field type: “M: $y = L$ ” to make the asymptote. You can edit it to be a different color and dashed if you would like.
3. In the “Input” field type: “P: $y = L/(1+b*e^{(-1*k*x)})$ ” to make the population function. You can edit it to be a different color if you would like.
4. In the “Input” field type “I: (0, P(0))” to make a point to show the population at time 0 (the initial population). Edit it so that under **Show Label** you select “Name and Value” or if you prefer, just “Value”
5. You can use the **Move Graphics View** button on the right to change the scale, but remember to switch back to **Move** tool when you are done to change the values on the sliders.